

DOING PHYSICS WITH MATLAB

MATHEMATICAL ROUTINES

TURNING POINTS OF A FUNCTION

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turningPoints.m

Matlab function to determine the turning points of a function. The function outputs in a Figure Window a plot of the function showing the maxima and minima points and displays in the Command Window the indices for the maxima and minima, and the x and y values at these points.

You are often required to find the stationary points of a curve where the gradient of the curve is zero. The function **turningPoints.m** can be used to find the stationary points corresponding to points of maxima and minima of a curve.

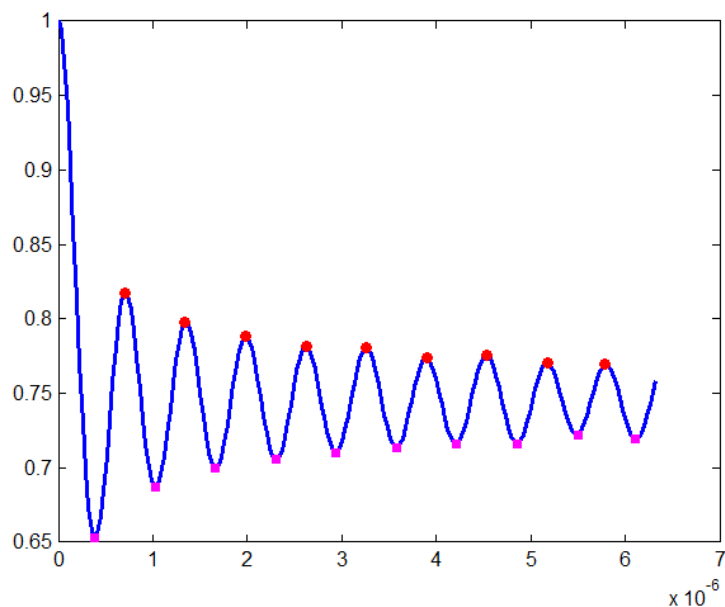
The x and y data for the curve are passed to the function in the Command window.

For example, **turningPoints(xP,WP)** is entered into the Command Window to pass on the variables xP (x data) and WP (y data) to the function **turningPoints.m**.

```
function turningPoints(xData, yData)
```

Sample results

Figure Window output: the maxima are marked as red dots and the minima are marked by magenta squares.



The indices and the x and y values are displayed in the Command Window.

Max values - indices / xData / yData

```
indexMax = 23 43 63 83 103 123 143 163 182
```

```
ans = 1.0e-05 *
```

```
0.0703 0.1342 0.1981 0.2621 0.3260 0.3899 0.4538 0.5177 0.5785
```

```
ans =
```

```
0.8174 0.7978 0.7886 0.7816 0.7804 0.7740 0.7760 0.7705 0.7693
```

Min values - indices / xData / yData

```
indexMin = 13 33 53 73 93 113 133 153 173 192
```

```
ans = 1.0e-05 *
```

```
0.0384 0.1023 0.1662 0.2301 0.2940 0.3579 0.4219 0.4858 0.5497  
0.6104
```

```
ans =
```

```
0.6527 0.6873 0.6998 0.7055 0.7104 0.7138 0.7160 0.7164 0.7223  
0.7190
```

mscript

```
function turningPoints(xData, yData)

size = length(xData);    %Get the length of the dataset

a1 = yData(1,1); a2 = yData(1,2);
if a2 > a1, flag = 1; else flag = 2; end;
v = 0;

% find max
for x = 2:size-1
    a1 = yData(1,x);    %Get two adjacent samples of the dataset
    a2 = yData(1,x+1);

    if flag == 1 && a2 > a1; x = x+1; end;
    if (flag == 1 && a2 < a1); v = v + 1; indexMax(v) = x; x = x+1;
end;
    if a2 <= a1, flag = 0; end;
    if a2 > a1, flag = 1; end;
end

a1 = yData(1,1); a2 = yData(1,2);
if a2 < a1, flag = 1; else flag = 2; end;
v = 0;

% find min
for x = 2:size-1
    a1 = yData(1,x);    %Get two adjacent samples of the dataset
    a2 = yData(1,x+1);

    if flag == 1 && a2 < a1; x = x+1;
end;
    if (flag == 1 && a2 > a1); v = v + 1; indexMin(v) = x; x = x+1;
end;
    if a2 >= a1, flag = 0; end;
    if a2 < a1, flag = 1; end;
end

figure(99)
plot(xData,yData,'lineWidth',2)
hold on

hp1 = plot(xData(indexMax),yData(indexMax),'o');
set(hp1,'MarkerEdgeColor','r','MarkerFaceColor','r','MarkerSize',5);

hp1 = plot(xData(indexMin),yData(indexMin),'s');
set(hp1,'MarkerEdgeColor','m','MarkerFaceColor','m','MarkerSize',4);

disp(' ')
disp('Max values - indices / xData / yData')
indexMax
xData(indexMax)
yData(indexMax)

disp(' ')
disp(' ')
disp('Min values - indices / xData / yData')
indexMin
xData(indexMin)
yData(indexMin)
```